

1. Find the 4x4 homogeneous 3D transformation matrix that translates by $(3, 5, 2)$, rotates by 45 degrees about the Z-axis, and finally, scales by $(3, 1, 2)$.
2. Suppose you wish to apply the transformation in question 1 to the normal vectors in a 3-D model. What is the transformation matrix that needs to be applied to the normal vectors in order to preserve the normals' perpendicular orientation relative to the surface of the object?
3. A triangular face, which is part of a larger 3-D model, is defined by vertices at the points $(1, 0, 1)$, $(3, 2, 4)$ and $(5, 3, 1)$
 - (a) If the convention is vertices for front-facing triangles are provided anti-clockwise, find the surface normal of the triangle defined by these three vertices.
 - (b) Explain why the normal vector at the vertices might not be set to the vector you found in part (a). What visual effect is this intended to produce?
4. Consider a scene with V vertices, N objects, and T triangles being rendered to a display with P pixels. Assuming a single fragment shader and no anti-aliasing, what is the upper bound of how many times the fragment shader will be run?
5. A bump/normal-mapped object can be made to appear bumpy when in fact the geometry is smooth. Given a bumpy-looking object, explain what characteristics can be used to determine whether the object has bumpy geometry or is making use of bump-mapping.
6. Explain why there are no colours lying outside of the curve formed by the pure colours in the CIE chromaticity diagram.